

See discussions, stats, and author profiles for this publication at: <https://www.researchgate.net/publication/253683133>

A Novel Clustering Algorithm Using Kmeans 'CUK'

Article in International Journal of Computer Applications · July 2011

DOI: 10.5120/2995-4025

CITATIONS

2

READS

53

2 authors, including:



Wesam Ashour

Islamic University of Gaza

64 PUBLICATIONS 518 CITATIONS

SEE PROFILE

Some of the authors of this publication are also working on these related projects:



Improved Spam Detection using DBSCAN and Advanced Digest Algorithm [View project](#)



Content-Based Image Retrieval [View project](#)

A Novel Clustering Algorithm using K-means (CUK)

Khaled W. Alnaji
The Islamic University of Gaza

Wesam M. Ashour
The Islamic University of Gaza

ABSTRACT

While K-means is one of the most well known methods to partition data set into clusters, it still has a problem when clusters are of different size and different density. K-means converges to one of many local minima. Many methods have been proposed to overcome these limitations of K-means, but most of these methods do not overcome the limitation of both different density and size in the same time. The previous methods success to overcome one of them while fails with the others. In this paper we propose a novel algorithm of clustering using K-means (CUK). Our proposed algorithm uses K-means to cluster data objects by using one additional centroid, several partitioning and merging process are used. Merging decision depends on the average mean distance where average distance between each cluster mean and each data object is determined, since the least and closet clusters in average mean distance are merged in one cluster, this process continues until we get the final required clusters in an accurate and efficient way. By comparing the results with K-means, it was found that the results obtained by the proposed algorithm CUK are more effective and accurate.

General Terms

Data Clustering, Unsupervised Classification.

Keywords

Data Clustering, K-means, Clustering using K-means, Average Mean Distance.

1. INTRODUCTION

Clustering is an unsupervised classification; the main goal of clustering is to group similar objects together so each group becomes cluster. While Objects in the same cluster should have the most similarity, they should also have the most different from other objects of clusters. A good clustering method will produce high quality clusters with high intra-cluster similarity and low inter-cluster similarity. The quality of a clustering result depends on both the similarity measure used by the method and its implementation and also by its ability to discover some or all of the hidden patterns [1].

There are widely used similarity and dissimilarity measures for different attribute types. Each types of data, including numerical data, categorical data, binary data, and mixed-typed data, has a measurement method.

Euclidean distance is probably the most common distance we have ever used for numerical data. For two data points x and y in d -dimensional space, the Euclidean distance between them is defined to be

$$d_{\text{eucl}}(x, y) = \sqrt{\sum_{j=1}^d (x_j - y_j)^2}$$

Where x_j and y_j are the values of the j th attribute of x and y , respectively [2].

Many of clustering algorithm was proposed to solve the clustering problem, we can classify these algorithm into partitioning and hierarchical [3]. Partitioning clustering algorithms try to determine K partitions that optimize a certain objective function.

In the other hand, a hierarchical clustering is a sequence of partitions in which each partition is nested into the next partition in the sequence.

K-means is one of the most commonly-used clustering algorithm which developed by Mac Queen in 1967. K-means is a simple and efficient partition clustering algorithm. It is most effective for relatively smaller data sets. K-means converges to one of many local minima because it minimizes a distance measure between each data and its nearest cluster center [4]. Many parallel versions of the K-means algorithm [5] use the basic serial K-means at their core. Besides, a number of stochastic clustering algorithms make use of the basic K-means or some of its variations.

The main problem of K-means is converging to the global optimal solution. Every time the K-means converges to local minima because of its greedy in nature, it is expected to converge to a locally optimal solution only and not to the global optimal solution. This problem is partially solved by applying the K-means in a stochastic framework like simulated annealing (SA) and genetic algorithm (GA) etc.

Unfortunately, K-means is so sensitive to initial starting points - centroids. If the initial partitions are not chosen carefully, the computation will run the chance of converging to a local minimum rather than the global minimum solution. Because of initial starting points generated randomly, K-means does not guarantee the unique clustering results [6].

It may be clear now that we can reach the global minimum if we run K-means more than one time until the partitions number be the same for many running time, of course this action has the drawback of being very time consuming and computationally expensive.

Moreover K-means has problems when clusters are of differing sizes, densities and non-globular shapes. Several methods were proposed to solve the cluster initialization of K-means.

In [7], a refinement approach is proposed, where starting with a number of initial samples of the data set we can obtain a number of sets of center vectors. These center vectors then pass through a refinement stage to generate a set of so called good starting vectors.

A variant of a recursive method for initializing the means by running clustering problems consists of taking the entire data and then randomly perturbing it K times [6].

In [8], a genetically guided K-means has been proposed where possibility of generation of empty clusters is treated in the mutation stage.

Another approach to initialize cluster centers based on values for each attribute of the data set has been proposed in [6]. These

methods are time costly and may not be applicable by keeping the K-means's inherently simple structure.

In [9] a new center vector computation strategy enables us to redefine the clustering process and to reach our goal. The modified algorithm is found to work very satisfactorily, with some conditional exceptions, which are very rare in practice.

In [10] the authors optimize the initial centroids for K-means. It utilizes all the clustering results of K-means in certain times, even though some of them reach the local optima. Then, we transform the result by combining with Hierarchical algorithm in order to determine the initial centroids for K-means.

Authors have used Principal Component Analysis (PCA) in [12] for dimension reduction and finding the initial centroid for K-means. They have used heuristics approach to reduce the number of distance calculation to assign the data point to cluster.

In [13] authors proposed the global k-means clustering algorithm, which constitutes a deterministic effective global clustering algorithm for the minimization of the clustering error that employs the k-means algorithm as a local search procedure.

In this paper, we will present a novel clustering algorithm using K-means (CUK). Our proposed algorithm tries to cluster data objects in accurate and efficient when clusters are of different size and different density.

In Section 2, we describe the K-means algorithm and distortion of the method. In Section 3, we propose CUK algorithm as a new approach to cluster data objects using K-means. Section 4 performs the experimental results on the artificial data set as well as real data set. In Section 5, we will draw conclusions.

2. RELATED WORK

The K-means algorithm [12] is very commonly used for clustering data. To handle a large data set, a number of different parallel implementations of the K-means have also been developed. Here, we shall provide a brief description of the serial K-means and some of its properties relevant for the current work.

In crisp partitional clustering, a set D of N patterns $\{x_1, x_2, \dots, x_N\}$ of dimension d is partitioned into K clusters denoted by $\{C_1, C_2, \dots, C_K\}$ such that the sum of within cluster dispersions, i.e., the Squared Error (SSE) , as given in (1), becomes the minimum.

Here, $M = \{M_1, M_2, \dots, M_k\}$ is the set of cluster mean.

$$SSE = \sum_{i=1}^K \sum_{x \in C_i} dist^2(m_j, x) \dots Equation (1)$$

2.1 A basic K-means algorithm

The basic K-means algorithm is commonly measured by any of intra-cluster or inter-cluster criterion. A typical intra-cluster criterion is the squared-error criterion (Equation 1). It is the most commonly used and a good measure of the within-cluster variation across all the partitions. For the current work, we consider intra-cluster squared-error function to evaluate the present scheme of clustering. In basic K-means algorithm, a set D of dimensional data is partitioned into K clusters, starting with a set of K randomly generated initial center vectors.

The process iterates through the following steps:

- Assignment of data to representative centers upon minimum distance, and
- Computation of the new cluster centers.

The process stops when cluster centers (or the SSE) become stable for two consecutive iterations.

Algorithm 1: Basic K-means Algorithm.

1. Initialize K center locations (C_1, \dots, C_k)
 2. Assign each X_i to its nearest cluster center C_i
 3. Update each cluster center C_i as the mean of all X_i that have been assigned as closest to it
 - 4.
 5. calculate $SSE = \sum_{i=1}^K \sum_{x \in C_i} dist^2(m_j, x)$
 6. If the value of SSE has converged, then return (C_1, \dots, C_k) ; else go to Step 2.
-

3. OUR PROPOSED ALGORITHM

Our proposed algorithm CUK uses K-means to cluster data objects when clusters are of different size and different density. We use K-means as a guide to find the optimal solution to assign data objects to the correct cluster. Thus CUK is classified as partitional clustering algorithm. CUK uses the average mean distance between each cluster mean and each data object as a metric to take decision of merging. The average mean distance acts as a measure of density of objects; the following formula was used to determine the Average Mean Distance (AMD)

$$AMD(C_k, M_j) = \frac{\sum_{j=1}^n \sum_{i \in C_k} d(X_j - M_j)}{N_k} \quad , k \neq j \dots Equation (2)$$

Where C_k is the kth cluster, M_j is the jth cluster mean, X_j is ith data object of X, n is the total number of data objects, N_k is the total number of data objects that belong to cluster C_k and $d(X_j - M_j)$ is the Euclidian distance between X_j and M_j .

In this proposed algorithm we try to reach the global optimal as possible as we can through multiple splitting using K-means and merging with respect to average mean distance. Initially CUK runs K-means with one additional centroid, and then we calculate the Average Mean Distance from each cluster mean. The two clusters with least AMD are merged into one cluster. It is important to exclude data objects that have shared in previous merging process, so they will not share in merging process next time. CUK continues in this manner for K times, where K is the cluster number. We will see in the next section that CUK does better than K-means in assignment data objects to clusters. CUK makes the assignment more accurate and efficient.

3.1 Proof of merging according to Average Mean Distance AMD:

Let us consider a 1-dimensional data set

$\{X_1 = 1, X_2 = 2, X_3 = 4, X_4 = 5, X_5 = 10, X_6 = 11, X_7 = 15, X_8 = 16, X_9 = 19, X_{10} = 20, X_{11} = 23, X_{12} = 25\}$.

Suppose that the required clusters are C1, C2. By using CUK algorithm, we run K-means with additional one centroid and thus we get three clusters C1, C2, and C3.

Table 1. Description of Clusters Cj

	Cluster 1	Cluster 2	Cluster 3
Cluster Members	X1, X2, X3, X4	X5, X6, X7, X8	X9, X10, X11, X12
Cluster Mean Mj	3	13	21.75

Table 1 shows the members of each cluster C_j along with the mean M_j .

At this stage we calculate the average mean distance for each cluster C_j , where C_j is the j th cluster, we get the following results:

Table 2. Average Mean Distance AMD of cluster C_j

AMD of cluster 2 from cluster 1 mean	10
AMD of cluster 3 from cluster 1 mean	18.75
AMD of cluster 1 from cluster 2 mean	10
AMD of cluster 3 from cluster 2 mean	8.75
AMD of cluster 1 from cluster 3 mean	18.75
AMD of cluster 2 from cluster 3 mean	8.75

Table 2 shows the average mean distance from each data objects of cluster C_j to each cluster mean M_j .

From the above table it is clear that the C2 and C3 have the closest average mean distance, so it is useful to merge C2 and C3 in one cluster and have C1 in a separate cluster. By generalizing this assumption, we get:

For a d -dimensional data set $\{X_1, X_2, X_3, \dots, X_n\}$ is partitioned into K clusters $C_1, C_2, C_3, \dots, C_k$. By using our proposed algorithm CUK we get the following clusters $C_1, C_2, C_3, \dots, C_k, C_{k+1}$, with Average Mean Distance $AMD_1, AMD_2, AMD_3, \dots, AMD_k, AMD_{k+1}$. Merging the least and closet two clusters will result the K clusters.

3.2 Implementation of proposed algorithm:

The following table shows the main implementation of CUK algorithm

Algorithm 2: Proposed Algorithm CUK.

1. K = number of clusters
2. for each cluster C_j
3. KN =number of clusters + 1
4. run K -means
5. get the closest clusters $C_a, C_b = \text{closest_cluster}()$
6. $\text{merge_cluster}(C_a, C_b)$
7. for each data objects X_i in cluster C_j
8. Update the list of data objects to include non-merging objects X include X_i with $\text{merge_flag}=0$
9. end
10. end
11. if $KN == K+1$
12. get the closest clusters $C_a, C_b = \text{closest_cluster}()$
13. $\text{merge_cluster}(C_a, C_b)$
14. end

The following table shows the implementation of closest_cluster procedure.

Procedure 1: Procedure Of closest_cluster

1. procedure $\text{closest_cluster}()$
2. {
3. for each cluster C_j
4. for each data objects X_i in cluster C_j
5. $\text{average_mean_distance} =$

$$\sum_{j=1}^k \times \sum_{jj=1; jj \neq j}^k \times \sum_i^n (X_j, M_j)$$

6. end
7. end
8. for each cluster C_j
9. find two clusters C_a, C_b with least and closet $\text{average_mean_distance}$
10. end
11. return C_a, C_b
12. }

The following table shows the implementation of merge_cluster procedure.

Procedure 2: Procedure Of merge_cluster

1. procedure $\text{merge_cluster}(C_a, C_b)$
2. {
3. if $\text{average_mean_distance}$ of $C_a >$
 $\text{average_mean_distance}$ of C_b
4. for each data objects X_i in cluster C_b
5. assign X_i to cluster C_a
6. merge_flag of $X_i=1$ to exclude X_i from the next merging process.
7. end
8. else
9. for each data objects X_i in cluster C_a
10. assign X_i to cluster C_b
11. merge_flag of $X_i=1$ to exclude X_i from the next merging process.
12. end
13. end
14. }

Initially CUK takes the number of cluster K as an input, after that we add one additional centriod, So the number of clusters $NK =$ number of clusters $(K) + 1$, After running K -means with NK we gets NK clusters with a mean M_j for each cluster. Now we compute the Average Mean Distance from each data object to each cluster mean M_j according to equation 2. The least and closet two clusters distance are determined. Merging decision depends on the density of cluster, by comparing which of the two clusters has the largest Average Mean Distance, we will merge cluster of less density (lowest Average Mean Distance) with the other of higher density (largest Average Mean Distance). At this stage we have a new cluster; this new cluster will not share again in splitting and merging process. It is important to specify which data objects should not share in merging process this can be done by putting the merge flag to one for each merging data objects. CUK makes feedback of those data objects, which do not share in merging process, and again runs K -means with these objects to get the best clustering. We check the number of resulting clusters K after running the CUK for $K+1$ times, it is possible to get one additional cluster. Additional cluster is due to the same Average Mean Distance of different clusters. In the case of additional cluster, simply get the average mean distance from each data object to each cluster mean M_j according to equation 2, the least and closet two cluster distance are determined. Now we compare which of them is more density (largest AMD) than other, merging cluster of less density (lowest AMD) with the other of higher density (largest AMD) so we get one cluster at the end. CUK repeats the previous steps for K iterations.

4. EXPERIMENTAL RESULTS

This section provides a comparison of the conventional K-means and our proposed algorithm CUK in terms of accuracy and the quality of the solution when clusters are of different size and different density.

In order to analyze the accuracy of our proposed algorithm, we apply CUK to two kinds of experiments: artificial data set and real data sets.

We represent Error percentage as performance measure in the experiments. It is calculated from number of misclassified patterns and the total number of patterns in the data sets.

$$\text{Error} = \frac{\text{Number of misclassified}}{\text{Number of Patterns}} \times 100\%$$

4.1 Artificial Data Sets

This kind of experiment can express the ability of the proposed algorithm CUK to solve clustering cases with artificial data sets. In the experiment, we use two-dimensional data set (x and y). Then, we use normrnd function in Matlab to generate the random artificial data sets. Two artificial data sets are considered for this experimentation. The artificial data sets are DATA_SET_1, and DATA_SET_2. For example, in DATA_SET_1, there are three clusters and 2 dimensions, while in DATA_SET_2; there are three clusters and 2 dimensions as shown in Table 3.

Table 3. Description of artificial data used

Data Sets	Data Size	Dimension	No. of clusters
DATA_SET_1	335	2	3
DATA_SET_2	156	2	3

We do clustering of the artificial data sets DATA_SET_1 and DATA_SET_1 with our proposed algorithm CUK and K-means.

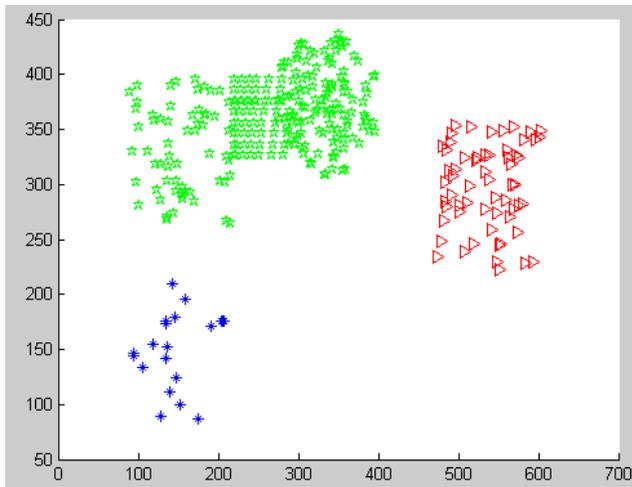


Fig 1. DATA_SET_1 clustered by proposed algorithm CUK

Figure 1 shows the result of clustering DATA_SET_1 using our proposed algorithm CUK. We have three clusters which are green cluster (denoted by stars), red cluster (denoted by triangles), and blue cluster (denoted by points). Green cluster is the largest one.

From the above figure, we see that CUK solves the problem of different size clusters in efficient way.

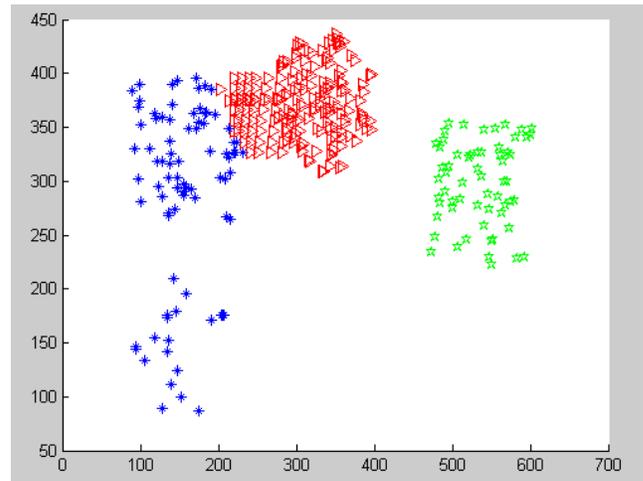


Fig 2. DATA_SET_1 clustered by K-means algorithm

Figure 2 shows the result of clustering DATA_SET_1 using K-means algorithm. We have three clusters which are green cluster (denoted by stars), red cluster (denoted by points), and blue cluster (denoted by triangles). From the above figure we see that K-means has problem when clusters are of different sizes. K-means fails in classification of red cluster and blue cluster, while our proposed algorithm success.

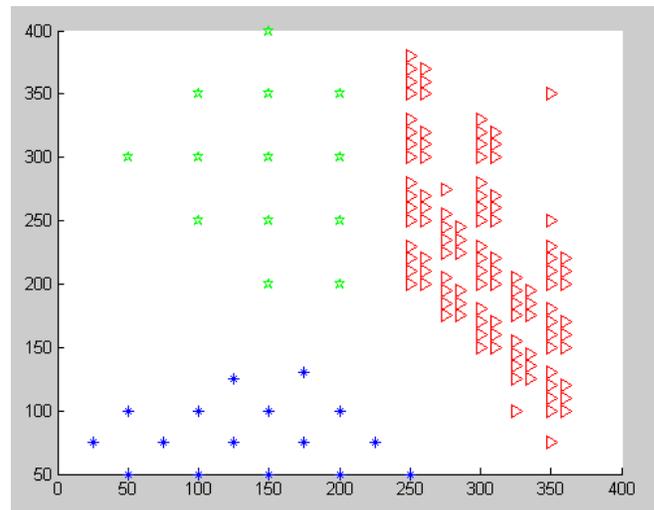


Fig 3. DATA_SET_2 clustered by proposed algorithm CUK

Figure 3 shows the result of clustering DATA_SET_2 using our proposed algorithm CUK. We have three clusters which are green cluster (denoted by stars), red cluster (denoted by triangles) and blue cluster (denoted by points). Blue cluster and green cluster have different density (AMDs), red cluster is denser (larger AMD) than both cluster blue and cluster green. From the above figure, we see that CUK solves the problem of clusters with different density (AMD) in efficient way.

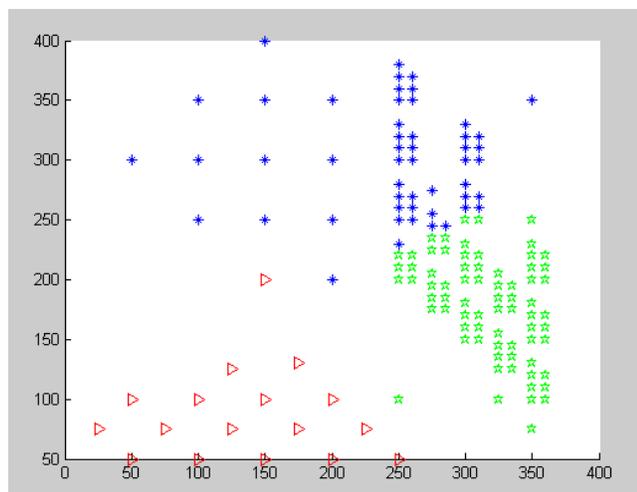


Fig 4. DATA_SET_2 clustered by K-means algorithm

Figure 4 shows the result of clustering DATA_SET_2 using K-means algorithm. We have three clusters which are green cluster (denoted by stars), red cluster (denoted by triangles), and blue cluster (denoted by points). From the above figure, we see that K-means has problem when clusters are of different dense (AMD). K-means fails in classification of green cluster and blue cluster, while our proposed algorithm success.

4.2. Real Data Sets

In order to analyze the accuracy of our proposed algorithm, we try to make experiments using a number of real data sets. The data sets, which we use, are Iris data, Glass data, and Haberman data.

4.2.1. Iris data set

We obtained this data set from UCI Repository. This data set contains information about Iris flowers. There are three classes of Iris flowers, namely Iris Setosa, Iris Versicolor and Iris Virginica. The data set consists of 150 examples with 4 attributes. One class is well separable the other two. The others have a large overlap.

4.2.2. Glass data set

We obtained this data set from UCI Repository. This data set contains information From USA Forensic Science Service; 6 types of glass; defined in terms of their oxide content (i.e. Na, Fe, K, etc). There are seven classes of glass, namely building_windows_float_processed, building_windows_non_float_processed, vehicle_windows_float_processed, vehicle_windows_non_float_processed (none in this database), containers, tableware and headlamps. The data set consists of 214 examples with 10 attributes.

4.2.3. Haberman data set

We obtained this data set from UCI Repository. This data set contains cases from study conducted on the survival of patients who had undergone surgery for breast cancer. There are two classes of Survival status, the patient survived 5 years or longer and the patient died within 5 year. The data set consists of 306 examples with 3 attributes. We used Error percentage to validate the results of our proposed algorithm. We compute the real data sets with our proposed algorithm CUK and K-means, after running them for 100 times we take the average results. The results of comparison are given in Table 4.

Table 4. The Error percentage comparison between our proposed algorithm CUK and K-means

Data Set	Used Algorithm	Error percentage (%)
Iris data set	Proposed Algorithm	16.67
	K-means	21.67
Glass data set	Proposed Algorithm	40.1215
	K-means	44.8598
Haberman data set	Proposed Algorithm	37.5817
	K-means	48.7124

Table 4 shows the Error percentage comparison between our proposed algorithm CUK and K-means. Using Iris data sets, our proposed algorithm CUK has Error percentage equals to 16.67 while K-means has Error percentage equals to 21.67; our proposed algorithm CUK has lower Error percentage than K-means.

With Glass data sets, our proposed algorithm CUK has Error percentage equals to 40.1215 while K-means has Error percentage equals to 44.8598; our proposed algorithm CUK has lower Error percentage than K-means.

Also experiment on Haberman data sets shows that our proposed algorithm CUK has Error percentage equals to 37.5817 while K-means has Error percentage equals to 48.7124; our proposed algorithm CUK has lower Error percentage than K-means.

From Table 4 and by referring to the experimental results on the real data sets, it can be observed that our proposed algorithm CUK has lower Error percentage than K-means. Since Error percentage is an indication of algorithm accuracy this means that our proposed algorithm CUK is better than K-means in clustering real data sets.

5. CONCLUSION

In this paper, we presented a novel algorithm for performing clustering using K-means (CUK) when clusters are of different size and different density. CUK used one additional centroid, the distance measurement depends on the density of data objects from all clusters mean. Our experimental results demonstrated that our scheme could do better than the conventional K-means algorithm. While our proposed algorithm solve the problems when clusters are of differing Sizes and Densities, the conventional K-means failed.

6. REFERENCES

- [1]. D.Vanisri, and Dr.C.Loganathan, "An Efficient Fuzzy Clustering Algorithm Based on Modified K-Means", D. Vanisri et. al. International Journal of Engineering Science and Technology Vol. 2(10), 2010, 5949-5958.
- [2]. S. Guha, R. Rastogi, and K. Shim, "CURE: An Efficient Clustering Algorithm for Large Databases", Proc. ACM SIGMOD Int'l Conf. Management of Data, ACM Press, New York, 1998, pp. 73-84.
- [3]. Gan, Guojun, Chaoqun Ma, and Jianhong Wu, Data Clusterin, "Theory, Algorithms, and Applications", ASA-SIAM Series on Statistics and Applied Probability, SIAM, Philadelphia, ASA, Alexandria, VA, 2007.

- [4]. H. Tsai, S. Horng, S. Tsai, S. Lee, T. Kao, and C. Chen. "Parallel clustering algorithms on a reconfigurable array of processors with wider bus networks", in Proc. IEEE International Conference on Parallel and Distributed Systems, 1997.
- [5]. I. S. Dhillon and D. S. Modha, "A Data-Clustering Algorithm on Distributed Memory Multiprocessors", in Proceedings of KDDWS on High Performance Data Mining, 1999.
- [6]. S. S. Khan and A. Ahmed, "Cluster center initialization for Kmeans algorithm", in Pattern Recognition Letters, vol. 25, no. 11, pp. 1293-1302, 2004.
- [7]. P. S. Bradley and U. M. Fayyad, "Refining Initial Points for Kmeans Clustering", in Technical Report of Microsoft Research Center, Redmond, California, USA, 1998.
- [8]. F. X. Wu, "Genetic weighted K-means algorithm for clustering large-scale gene expression data", in BMC Bioinformatics, vol. 9, 2008.
- [9]. Malay K. Pakhira, " A Modified K-means Algorithm to Avoid Empty Clusters", International Journal of Recent Trends in Engineering, Vol 1, No. 1, May 2009.
- [10]. Kohei Arai, and Ali Ridho Barakbah, "Hierarchical K-means: an algorithm for centroids initialization for K-means", Saga Univ. Saga University, Vol. 36, No.1, 2007.
- [11]. Tajunisha and Saravanan, "Performance analysis of K-means with different initialization methods for high dimensional data", International Journal of Artificial Intelligence & Applications (IJAI), Vol.1, No.4, October 2010.
- [12]. J. B. McQueen, "Some methods of classification and analysis in multivariate observations", in Proc. Of fifth Barkley symposium on mathematical statistics and probability, pp. 281 - 297, 1967.
- [13]. Likas, Vlassis and J. J. Verbeek, "The global k-means clustering algorithm", in Pattern Recognition , vol. 36, no. 2, pp. 451-461, 2003.